

# Calculating Locational Tolerances

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# 1 Introduction

## 1.1 Objective

Location tolerances are required to ensure that parts, and their fasteners, fit together and that features are located to within specification. What follows is a systematic procedure for determining locational tolerances for bolts, screws, pins, shafts, and features embedded on the parts. This document is intended as a guide for designers, drafters and drawing checkers.

The terminology used in this document will be familiar to anyone who has read up on or is trained in Geometric Dimensioning and Tolerancing (GD&T).

## 1.2 Copyright

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## 1.3 Change History

1998 Sep 14: First issue.

1998 Dec 01: Clarified some text. Expanded Positional Tolerances section a bit.

1999 Aug 24: Added a web page reference. Typo correction.

2000 Jul 20: Cleaned up the HTML formatting a bit. No change in text.

2000 Aug 27: Clean up HTML some more, finally getting background colour to work. Maximum error for datum dimensioning was  $45^\circ$  opposite to each other. The section of precise geometric tolerancing make a little clearer.

2005 Jul 20: Rewrote GD&T section.

2006 Apr 29: Reformatted L<sup>A</sup>T<sub>E</sub>X code. No change to content.

2007 Oct 31: Deleted section *Zero Tolerance Applied Without MMC*

2010 Jun 01: Added Implied  $90^\circ$  subsection. Moved the zero positional tolerance section to the Appendix, and wrote the Positional Tolerance from First Principles section.

2010 Jun 02: A couple of minor corrections.

2014 Jul 04: Corrected Figure 5

2015 Jan 02: Corrected Figure 6 and Figure 7 Finally ran spellcheck. Only two corrections! :)

2016 Apr 23: Fixed four bolt pattern equation. Clarified equations for Datum Dimensioning Added a figure for Datum Patterns.

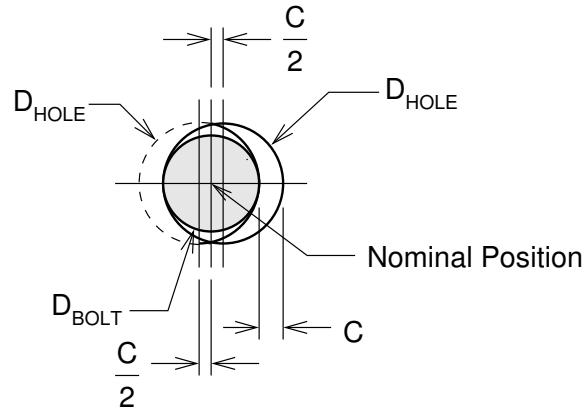


Figure 1: Bolted Connection – worst case

## 2 Modelling

When parts are held together by more than one fastener, the tolerances for the holes must ensure not only that the parts are located to within specification, but also that all the fasteners can be installed. Analysis will consist of determining the maximum possible location error that will allow this, and then working out the equivalent drawing tolerance. It will be assumed that all holes are drilled, punched, tapped or whatever, prior to assembly. If the tolerances generated by the following calculations are not reasonable, drilling at assembly may be the only solution.

The analysis will cover a series of fastener configurations and dimensioning procedures. For the purposes of building analysis models, fastener assemblies can be split up into two categories, which will be termed here “bolts” and “screws.” For each of these, we can determine a maximum acceptable error, and for each design configuration, and for each style of tolerance application on the drawing, we can work out the tolerance.

### 2.1 Bolts

Fasteners pass through clearance holes in both parts. The obvious example of this is a nut and bolt assembly, but this could also be a cotter pin assembly or a pre-drilled rivet assembly. The bolts could be clamping more than two parts at a time.

See Figure 1 . It will be assumed for analysis purposes, that bolts are located precisely at their nominal position. The two clearance holes are shifted off the nominal position such that their edges just touch the bolt, on opposite sides. This is the maximum acceptable error condition. If the clearance in each hole at MMC is  $c$ , then...

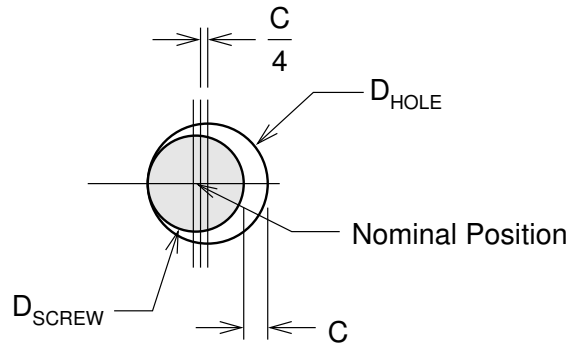


Figure 2: Screwed Connection – worst case

Maximum allowable shift of holes for bolting:

$$\Delta_b = \frac{c}{2} \quad (1)$$

## 2.2 Screws

Fasteners pass through a clearance hole in one part, and are solidly located in the other part. These could be screws sitting in tapped holes, or they could be dowel pins, or features integral to one of the parts. As with a bolted assembly, a screw could be holding more than one piece to its base.

See Figure 2. The screw and clearance hole have moved in opposite directions, such that the screw is touching the edge of the hole. If  $c$  is the clearance in each hole at MMC, then...

Maximum allowable shift of holes for screwing:

$$\Delta_s = \frac{c}{4} \quad (2)$$

A screw assembly allows only half the error of a bolted assembly. This is something to consider if the location tolerances are difficult to maintain.

## 2.3 Positional Error

The ASME Y14.5 standard recommends the use of positional tolerances for locating features of size, with a secondary preference for profile tolerances. Much of this article looks at  $\pm$  tolerances for locating holes. This was the original purpose of the article. People still use this notation for tolerances, and it is defined under the ASME standard, so as design checker, you can accept it if it

works. If you are designing or drafting, you will see from this article that positional tolerances are the better way.

For two dimensional configurations, it will usually be assumed that the maximum error occurs at a  $45^\circ$  angle. The assumption is that the fabricator's capability is equal in both the  $x$  and  $y$  directions. If this assumption is *not* true for a given application, then the angle, and the resultant calculations and tolerances can be fudged a bit, although, not very much.

### 3 Fastener Configurations

The tolerance that must be applied on a drawing feature depends on the configuration of the fasteners and on the dimensioning procedure. Most articles on *ASME Y14.5 Dimensioning and Tolerancing* point out that GD&T provides a maximum of allowance for a given part. This is important if the tolerance to be achieved is difficult, and if an increase in allowance can reduce costs. If tolerances are fairly easy, then the cost of preparing and reading the drawings must be considered. Regardless of how the tolerances are applied, GD&T provides a precise interpretation of how the tolerances are to be determined from the dimensions.

#### 3.1 Implied $90^\circ$ Angles (Warning, Warning, Warning!)

See Figure 3 . ASME Y14.5-2009 paragraph 2.1.1.3<sup>1</sup> states that undimensioned angles that appear to be  $90^\circ$  are to be assumed to be  $90^\circ$ . The tolerance of an undimensioned orthogonal feature is the value specified on your default tolerance notes. On most drawings, this is something like  $\pm 0.5^\circ$ , or  $\pm 1^\circ$ .

If holes are located from an edge with  $\pm$  tolerances, consider the possibility that the edge is not perpendicular to the base. Do you measure from the straight line that contacts the two outside points of the edge? Do you measure from the nearest part of the edge?

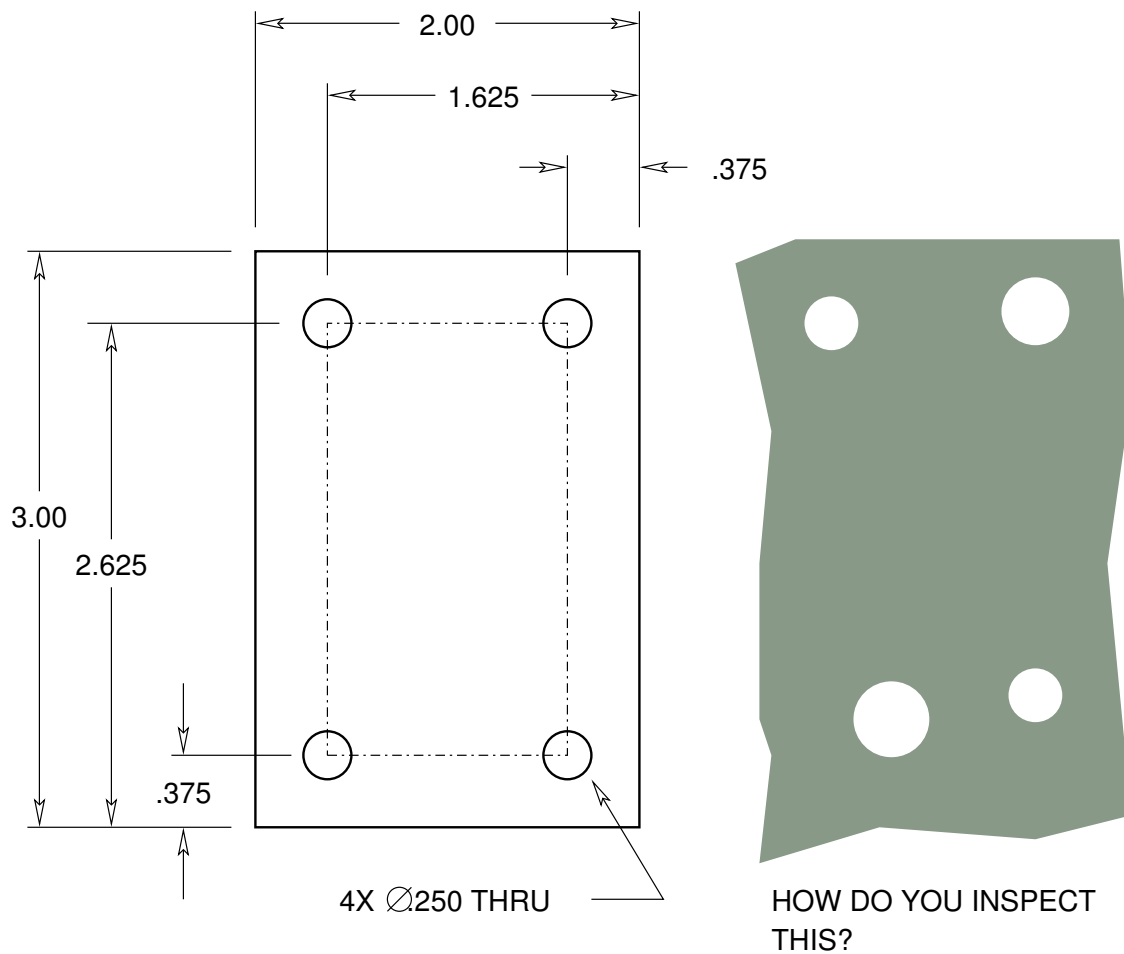
This is not an issue with GD&T positional tolerances, since everything is located from the orthogonal datums you specified. Using a profile tolerance to control the outline of your part is good practice.

If you are checking drawings prepared with  $\pm$  tolerances, you will have to decide how willing you are to argue with the drafter or designer. A machine or sheet metal shop that wants repeat business is not going to deliver parts  $1^\circ$  out of perpendicular, even if the drawing allows it.

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<sup>1</sup> On ASME Y14.5M-1994 this is paragraph 2.1.1.2. I don't know about the ISO GD&T standard.





UNLESS OTHERWISE SPECIFIED, ALL  
DIMENSIONS ARE IN INCHES.  
DIMENSIONS AND TOLERANCES ARE AS  
PER ASME Y14.5M-2009.  
0.00  $\pm$  0.05  
0.000  $\pm$  0.005  
ANGLES:  $\pm$ 1°

Figure 3: Datum Pattern

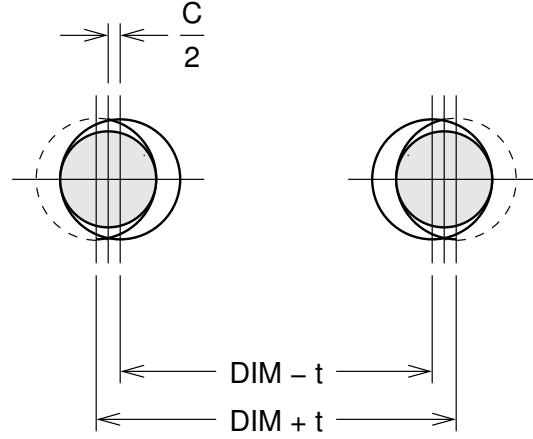


Figure 4: Attachment with two bolts

### 3.2 Only Two Fasteners

Parts are assembled with two fasteners. It is assumed that the parts are not located accurately to each other. On the drawings, the holes are dimensioned from each other, rather from a datum.

In Figure 4, the maximum error occurs at both holes, so that tolerance is double the error. . .

$$t_b = 2 \times \Delta_b = 2 \times \frac{c}{2}$$

Tolerances for dimensions between two bolts

$$\boxed{t_b = c} \quad (3)$$

$$t_s = 2 \times \Delta_s = 2 \times \frac{c}{4}$$

Tolerances for dimensions between two screws:

$$\boxed{t_s = \frac{c}{2}} \quad (4)$$

### 3.3 Four Fastener Pattern

Parts are assembled with four fasteners. Again, the relative location of the parts is not critical. On the drawing, the holes are dimensioned with respect to each other as shown in Figure 5.

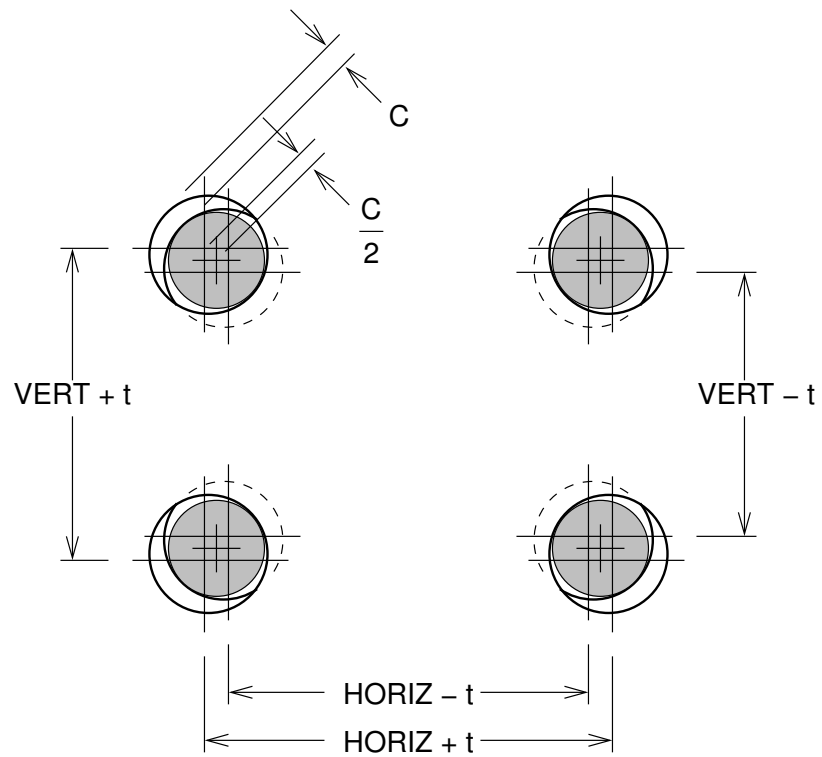


Figure 5: Attachment with Four Bolts in a Rectangle

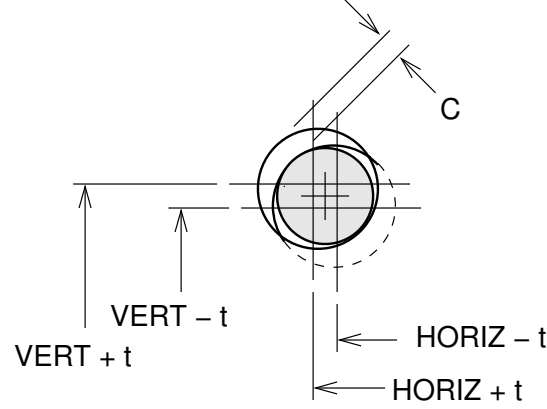


Figure 6: Bolts located from a Datum

The holes in Figure 5 are shown shifted the maximum distance, at a  $45^\circ$  angle. Again, the error occurs at each hole.

$$t_b = 2 \times \frac{\Delta_b}{\sin 45^\circ} = 2 \times \frac{c/2}{\frac{1}{\sqrt{2}}} = \sqrt{2} \times c$$

The tolerance for dimensions between four bolts:

$$\boxed{t_b = 1.414c} \quad (5)$$

$$t_s = 2 \times \frac{\Delta_s}{\sin 45^\circ} = 2 \times \frac{c/4}{\frac{1}{\sqrt{2}}} = \frac{\sqrt{2} \times c}{2}$$

The tolerance for dimensions between four screws:

$$\boxed{t_s = \frac{c}{1.414}} \quad (6)$$

### 3.4 Datum Dimensioning

Parts are assembled with any number of fasteners. On the fabrication drawings, all the holes are dimensioned from arbitrarily selected X and Y datums<sup>2</sup>. For one-off parts, this is popular with machine shops (and therefore cheaper) because only one set-up is required to locate all the holes.

<sup>2</sup>According to the Oxford Concise Dictionary, the plural of datum is “data”. This doesn’t parse very well. Fortunately, Webster’s Ninth New Collegiate Dictionary allows “datums.”

If the two parts are to be located accurately the holes must be registered to some feature other than another fastener hole. On any non-rectangular hole pattern with more than two holes, the dimensioning is effectively datum, even if everything is referenced from one of the holes.

The model assumes that two holes are located from datums. Each hole can shift in two dimensions, even if the holes are arrayed in a single line. It is assumed that the maximum error occurs when both holes shift to the maximum allowed, in opposite directions.

$$\begin{aligned}\Delta_b^2 &= \left(\frac{c}{2}\right)^2 = 2 \times t_b^2 \\ \frac{c^2}{4} &= 2t_b^2 \\ \frac{c^2}{8} &= t_b^2\end{aligned}$$

The tolerance for a datum dimension to a bolt hole:

$$\boxed{t_b = \frac{c}{2.828}} \quad (7)$$

$$\begin{aligned}\Delta_s^2 &= \left(\frac{c}{4}\right)^2 = 2 \times t_s^2 \\ \frac{c^2}{32} &= t_s^2\end{aligned}$$

The tolerance for a datum dimension to a screw hole:

$$\boxed{t_s = \frac{c}{5.657}} \quad (8)$$

### 3.5 Pitch Circles

The fasteners are located at specified positions around a circle, as shown in Figure 7. This model is similar to the datum dimensioning in that each fastener is located from a datum by two dimensions.

For a bolted assembly, the total error must not exceed  $\Delta_b$ . This error is a combination of  $t$ ,  $\tau$ , and  $D$ . Since the dimension tolerance  $t$  acts on the diameter, the effective allowance due to the specified  $t$  is  $t/2 \dots$

$$\Delta_b^2 = \left(\frac{c}{2}\right)^2 = \left(\frac{t_b}{2}\right)^2 + \left(\frac{D}{2} \tan \tau_b\right)^2$$

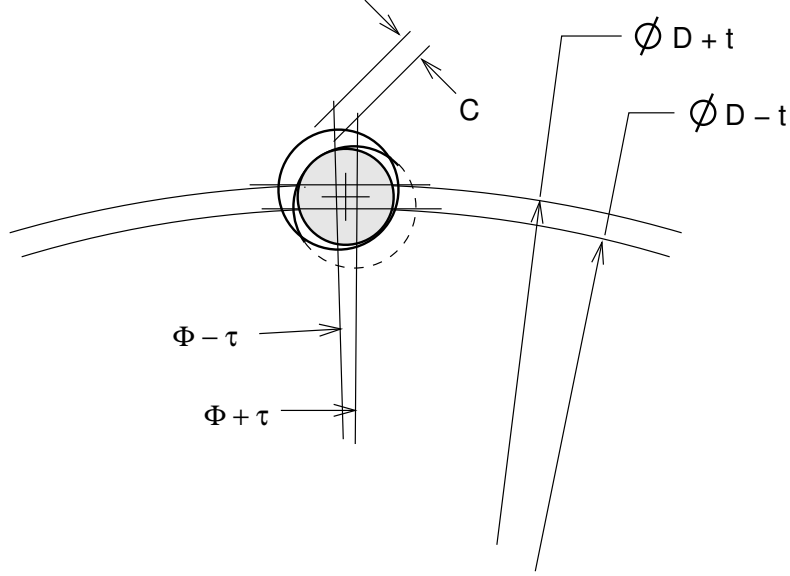


Figure 7: Bolts arrayed on a Pitch Circle

The simplest solution to this is to assume that the maximum allowable error acts at a  $45^\circ$  angle from the radial. In this case, the effective diameter error equals the effective angular error...

$$\frac{1}{2} \left( \frac{c}{2} \right)^2 = \left( \frac{t_b}{2} \right)^2 = \left( \frac{D}{2} \tan \tau_b \right)^2$$

$$\frac{c^2}{8} = \frac{t_b^2}{4} = \frac{1}{4} D^2 \tan^2 \tau_b$$

$$\frac{c^2}{2} = t_b^2 = D^2 \tan^2 \tau_b$$

$$t_b^2 = \frac{c^2}{2} \quad \text{and} \dots \quad \tan^2 \tau + b = \frac{c^2}{2D^2}$$

$$t_b = \sqrt{\frac{c^2}{2}} \quad \text{and} \dots \quad \tau + b = \arctan \sqrt{\frac{c^2}{2D^2}}$$

For a bolted assembly arranged on a pitch circle, the diametral and angular tolerances are...

$$\boxed{t_b = \frac{c}{1.414} \quad \text{and} \dots \quad \tau_b = \arctan\left(\frac{c}{1.414D}\right)} \quad (9)$$

For a screwed assembly, the total error must not exceed  $\Delta_s$ ...

$$\Delta_s^2 = \left(\frac{c}{4}\right)^2 = \left(\frac{t_s}{2}\right)^2 + \left(\frac{D}{2} \tan \tau_s\right)^2$$

Again, we assume that the maximum allowable error occurs at  $45^\circ$ .

$$\frac{1}{2} \left(\frac{c}{4}\right)^2 = \left(\frac{t_s}{2}\right)^2 = \left(\frac{D}{2} \tan \tau_s\right)^2$$

$$t_s = \sqrt{\frac{c^2}{8}} \quad \text{and} \dots \quad \tau_s = \arctan \sqrt{\frac{c^2}{8D^2}}$$

For a screwed assembly arranged on a pitch circle, the diametral and angular tolerances are...

$$\boxed{t_s = \frac{c}{2.828} \quad \text{and} \dots \quad \tau_s = \arctan\left(\frac{c}{2.828D}\right)} \quad (10)$$

### 3.6 A more elaborate pitch circle model

In the above system, the angular tolerance must be tightened as the diameter increases. At some magnitude of diameter, this will be too tight for fabrication at an acceptable cost. There are several ways around this.

- Do not specify pitch circles. Use datum dimensioning. Linear dimensions are not sensitive to increasing size. Fabricators often re-calculate pitch circles as datum dimensions anyway, since this is more suitable for their machinery. Datum dimensions are also easier to inspect.
- Use GD&T positional tolerances.
- Replace the holes with slots, with the long dimension arranged along the pitch circle. This is economical if the part is being punched.
- Fudge the above calculations by opening up the angular tolerance a bit and closing the diametral tolerance to make up for it.

If on a bolted pitch circle  $\frac{D}{2} \tan \tau_b < \Delta_b = \frac{c}{2} \dots$

... then you can select a slightly larger angular tolerance and recalculate the diametral tolerance...

$$\dots \left(\frac{c}{2}\right)^2 = \left(\frac{t_b}{2}\right)^2 + \left(\frac{D}{2} \tan \tau_b\right)^2$$

$$\left(\frac{t_b}{2}\right)^2 = \left(\frac{c}{2}\right)^2 - \left(\frac{D}{2} \tan \tau_b\right)^2$$

$$t_b = 2\sqrt{\left(\frac{c}{2}\right)^2 - \left(\frac{D}{2} \tan \tau_b\right)^2}$$

If on a screwed pitch circle

$$\frac{D}{2} \tan \tau_s < \Delta_s = \frac{c}{4} \dots$$

... then you can select a slightly larger angular tolerance and recalculate the diametral tolerance...

$$\dots t_s = 2\sqrt{\left(\frac{c}{4}\right)^2 - \left(\frac{D}{2} \tan \tau_s\right)^2}$$

You don't gain much by all this calculation. If you are having problems, you should really consider datum dimensions.

## 4 GD&T Positional Tolerances

The GD&T positional tolerance defines a tolerance zone within which the centre of the hole must be located. The hole is located with respect to one or more datums.

In most cases, this is exactly what you want to specify, so positional tolerances ought to be the preferred method.

There are several ways to apply tolerances to holes and to their positions.



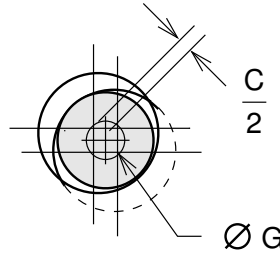


Figure 8: Bolt Located by a Positional Tolerance

#### 4.1 Positional Tolerances Using the Bolt and Screw Models

See Figure 8 .  $G$  is the positional tolerance to be called up on the drawing for a bolted assembly.  $c$  is the diametral clearance.

$$G_b = 2 \times \Delta_b = 2 \times \left( \frac{c}{2} \right)$$

For a bolted assembly, the geometric tolerance is ...

$$\boxed{G_b = c} \quad (11)$$

For a screwed assembly...

$$\dots G_s = 2 \times \Delta_s = 2 \times \left( \frac{c}{4} \right)$$

For a screwed assembly, the geometric tolerance is...

$$\boxed{G_s = \frac{c}{2}} \quad (12)$$

#### 4.2 Positional Tolerances from First Principles

Let's ignore the bolt and screw models preceding.

We want to install a fastener, and we want the clearance holes to clear it. In the following analyses, we assume that the parts are located by datums A, B and C which are external to the hole pattern.

##### 4.2.1 Bolt from First Principles

We locate our bolt at the exact nominal position.

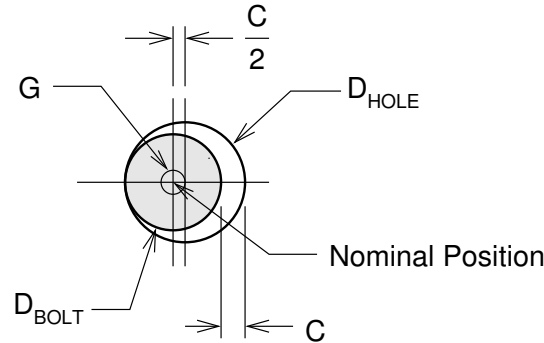


Figure 9: Bolted Connection with maximum position error



Figure 10: Specification of Figure 9's Geometry

Located exactly at nominal position, an infinitesimally larger clearance hole will clear the bolt. As the hole gets larger, it can shift some distance off nominal and still clear the bolt, as shown in Figure 9. Note that the geometric tolerance  $G$  applies to the hole, only.

Figure 10 shows the dimension specification we want to use on each part that requires a clearance hole. The zero positional tolerance applies only at MMC, the minimum clearance diameter. In the LMC case, you have the maximum sized hole, shifted the maximum clearance off to one side. The maximum diameter allows for the off-centre error as well as the error in the hole diameter.

$$\boxed{MIN_{BOLT} = D_{BOLT} + \text{minimum clearance}} \quad (13)$$

The hole *must* be larger than the bolt.

For our maximum diameter, we must allow for a reasonable positional tolerance  $G$  plus a reasonable tolerance on the hole diameter which would be  $\pm t$ .

$$\boxed{MAX_{BOLT} = MIN_{BOLT} + G + 2t} \quad (14)$$

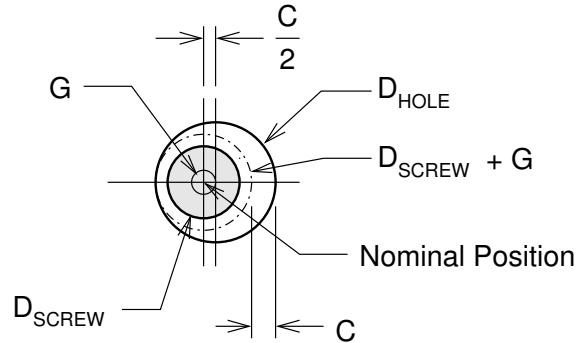


Figure 11: Screwed Connection with maximum position error

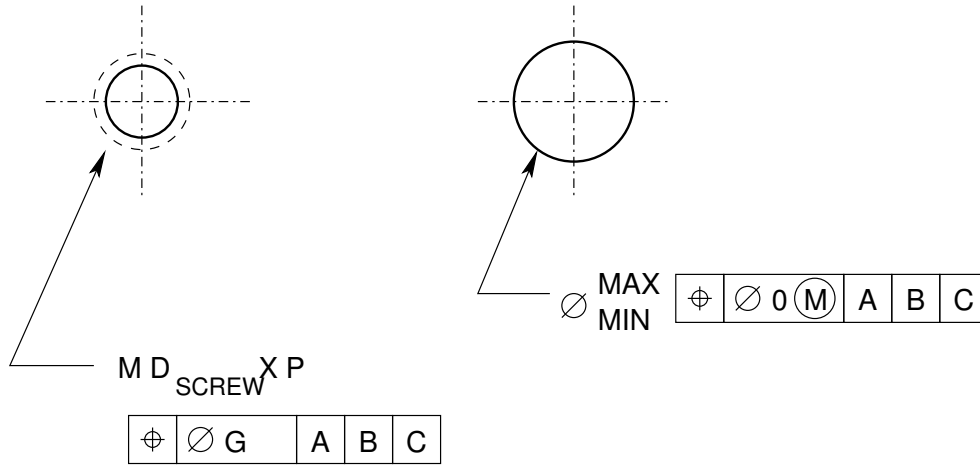


Figure 12: Tapped hole and clearance hole with positional tolerances

#### 4.2.2 Screw From First Principles

See Figure 11. For simplicity, we assume that the positional tolerance  $G$  is the same for the tapped hole and the clearance hole.

Our two parts require the dimension specifications shown in Figure 12. The tapped hole shown is metric, with a major diameter of  $D_{SCREW}$  and a pitch  $P$  which is not used on these calculations.

The screw is potentially able to occupy a space of  $D_{SCREW} + G$ , as shown on Figure 11. The clearance hole must clear this.

$$\boxed{MIN_{SCREW} = D_{SCREW} + G} \quad (15)$$

The positional tolerance of the tapped hole controls from the part's surface to the bottom of the tapped hole. Your clearance hole must clear whatever sticks *out* of the tapped hole. If your clearance hole goes through a thick plate, you should add a projected tolerance zone to your feature control frame, or at least, increase  $MIN_{SCREW}$  a bit.

Specifying MMC on a tapped hole makes no sense to me. Tapped holes are self-centreing, so there is no bonus tolerance!

For the clearance hole, again, we add a reasonable positional tolerance  $G$ , and the clearance hole tolerance  $\pm t$  to get...

$$\boxed{MAX_{SCREW} = MIN_{SCREW} + G + 2t} \quad (16)$$

It is not necessary for the positional tolerance  $G$  to be identical for the tapped hole and the clearance hole. If the tapped hole is in a machined part and the clearance is in a sheet metal part or a weldment, an accurate  $G_{TAP}$  will allow for a sloppier  $G_{CLEAR}$ . Or, vice versa!

#### 4.2.3 Checking Zero Positional Tolerances

If you are checking a drawing dimensioned like Figure 10, you can verify that the tolerance is fabricatable.

$$G + 2t = MAX - MIN$$

Obviously, maximally tight values for  $G$  and  $\pm t$  should not exceed the difference between  $MAX$  and  $MIN$ .

### 4.3 Calculations from ASME Y14.5M-1994 Appendix B

ASME Y14.5M-1994 proposes the fixed fastener case, equivalent to my bolts, and the floating fastener case, equivalent to my screws.

- $D$  = minimum depth of thread or minimum thickness of part with restrained or fixed fastener
- $H$  = maximum diameter of fastener (MMC limit)
- $F$  = minimum diameter of clearance hole (MMC limit)
- $P$  = maximum thickness of part with clearance hole, or maximum projection of fastener, such as a stud.
- $T$  = positional tolerance diameter

The floating fastener case...

$$H = F + T$$

or...

$$T = H - F$$

The fixed fastener case...

$$H = F + 2T$$

or...

$$T = \frac{H - F}{2}$$

An interesting problem came up on Eng-Tips forums, <http://www.eng-tips.com>. We are assembling two parts, one of which was designed and manufactured outside. We control the dimensions and tolerances only of the other part. The device is assembled using screws and nuts, so the floating fastener case applies. We can modify the equation for two sets of tolerances as follows...

$$H_1 + H_2 = 2F + T_1 + T_2$$

The manufactured part has a clearance hole  $H_1 = 0.104''$  and they have specified an orthogonal tolerance of  $\pm 0.005''$ . This is equivalent to a geometric tolerance of  $T_1 = 0.014''$ .

Let's set  $T_2 = 0$ , and solve for  $H_2$ .

$$\begin{aligned} H_2 &= T_2 + T_1 + 2F - H_1 \\ &= 0 + 0.014'' + 2 \times 0.086'' - 0.104'' \\ &= 0.082'' \end{aligned}$$

The calculated clearance hole is smaller than the screw!

Let's try again, setting  $H_2 = .086''$ , and solving for  $T_2$ .

$$\begin{aligned} T_2 &= H_1 + H_2 - 2F - T_1 \\ &= 0.104'' + 0.086'' - 2 \times 0.086'' - 0.014'' \\ &= 0.004'' \end{aligned}$$

Now the result makes sense. If you provide a zero clearance hole, you may allow a  $0.004''$  positional tolerance. This violates our standard model in which the bolt is located at the exact nominal position, but it is a perfectly functional assembly.

When you solve this problem, solve for the tolerance, not the hole diameter.

## 5 Example

Take the case that we have a 1/4-20UNC screw, and a clearance hole of 9/32 DIA. Work out the tolerance for a datum dimension, and for a GD&T positional tolerance. Assume that the hole is drilled, and that it will be bigger than nominal.

$$c = 9/32'' - 1/4'' = .03125''$$

Datum Tolerance:  $t_s = c/5.657 = .03125''/5.657 = .0055'' \approx .005''$

Positional Tolerance:  $G_s = c/2 = .03125''/2 = .0156'' \approx .015''$

From this, we can see that the datum tolerance of .005'' allows the same maximum error as a positional tolerance of .015''. The positional tolerance zone works out to  $.015''^2 \times \pi/4 = 1.8 \times 10^{-4}\text{in}^2$ . The tolerance zone of the datum tolerance is  $(2 \times .005'')^2 = 1 \times 10^{-4}\text{in}^2$ .

For a given acceptable error, the GD&T positional tolerance provides almost double the allowance for locating holes. If your manufacturing process is marginally capable of meeting tolerances, this will affect your scrap rate. Positional tolerances are also nice on drawings for formatting reasons. You attach the location tolerance to the hole specification, rather than to a dimension line, which may point to several different holes, with different tolerance requirements.

The old, linear tolerances are still simpler on the drawing, and the extra allowance is irrelevant if your manufacturing process easily exceeds the required accuracy.

Let us continue with the problem, this time assuming that the fabricator can locate holes to within a .010'' diameter, and drill holes in to  $\pm .005''$ . We will specify a positional tolerance of zero at MMC, and work out reasonable MAX and MIN diameters of the clearance hole.

$$\text{MIN} = D + G = 0.250'' + .010'' = 0.260''$$

$$\begin{aligned} \text{MAX} &= \text{MIN} + 2t \\ &= 0.260'' + 2 \times 0.005'' \\ &= 0.280'' \end{aligned}$$

The 1/4-20UNC hole will be located to a positional tolerance of .010''. The clearance hole will be .280/.260'', located to zero at MMC.

## 6 Closing Remarks

One thing to consider when applying tolerances to fabrication drawings, is the actual capability of your fabricators. The author has inspected parts fabricated in a machine shop. The observed location errors for holes were typically within 0.003 in. ( $\oplus .006$ ). This was close to the accuracy of the vernier equipment that was used, so a significant part of this was measurement error.

The author has not checked sheet metal, castings or weldments with similar thoroughness.

He has been told by a sheet metal fabricator, that sheet metal holes can be located to within .015" with respect to a folded edge. This fabricator is skilled, so other shops may not be as good.

Check out the D.S.M. Manufacturing Company's web page for more sheet metal tolerances. For their sheet metal, they quote  $\pm .003$ in for hole diameters, and  $\pm .005$ in for hole to hole locations in parts that do not have too many holes punched in them. They would prefer it if designers allowed  $\pm .010$ in. Hole to fold tolerances should be  $\pm .015$ in, and fold to fold tolerances should be about  $\pm .020$ in.

The D.S.M.'s web page is at...

<http://www.precisionsheetmetal.com>

One objective of toleranceing, particularly geometric toleranceing, is to control costs by allowing as much variance as possible. This can reduce scrap rates by increasing the probability that fabricated parts conform to specification. This might reduce fabrication costs by allowing the fabricator to work faster, or use a cheaper manufacturing process.

Another possibility is that the standard manufacturing process can easily achieve the specified tolerances. In this case, a complicated drawing may increase the cost as the fabricator takes the extra time required to interpret the dimensions, and for that matter, as the designer takes the extra time required to produce the drawing! This is particularly true for one-off items, and for items requiring complete inspection, and any other situation that imposes frequent reference to the fabrication drawings.

The designer must balance the cost of managing the drawings against the need for loose, easily met specifications.

## A Older GD&T Notes

The following sections were under GD&T Positional Tolerances in earlier versions of this document. These notes are correct, but not particularly readable. I think my current notes show a better system.

### A.1 Positional Tolerances with Zero Positional Error

The hole specification shown in Figure 10 looks scary at first glance. Actually, it is an optimal way to specify a hole and positional tolerance. It allows a maximum amount of fabrication error, while assuring a functional part.

The total error is a composite of the positional error and the error in the diameter of the hole. Your fabricator is presented with an error budget which they can manipulate to use the most efficient and reliable process possible.

The zero tolerance applies at MMC, the MIN diameter. The allowable error increases with diameter with the maximum allowable occurring at diameter MAX.

The bolt is assumed to be located exactly at the nominal position.

When both holes are at MIN diameter, they must be located with zero positional error. The bolt fits exactly through the holes.

Figure 8 illustrates the general case where there is a positional tolerance of  $G$  and a diametral clearance  $c$ . When both holes are a MAX diameter, a maximum value of  $G$  applies.

If we did not call up maximum material condition in the location tolerance, the maximum sized holes would have to be located with zero positional error. From a practical point of view, this is desirable, however, we cannot avoid the case where the bolt shifts off to one side of the hole. If both holes are at maximum, there is no control over the position of the bolt. In a bolted assembly, the worst case is always that the bolt is all the way to one side in the hole. You might as well specify the sloppier, easier to fabricate MMC.

#### A.1.1 Positional Tolerances for Bolts with Zero Positional Error

We have a bolt with diameter  $D$ . We are calling up the clearance holes as per Figure 10 .

Since bolts are always undersized, they will always pass through a hole equal to the bolt's nominal diameter.

$$\text{MIN} = D$$

A hole of size  $\text{MIN}$  must be located exactly at nominal if a bolt of size  $D$  is to pass through it.

For design purposes, we arbitrarily assign a value to diameter MAX. Presumably, we want to leave adequate material under the head of the bolt and/or washer, or we have an acceptable play for a pin and clevis.

We want to work out the accuracy the fabricator requires to achieve the tolerance.  $G_{fab}$  is the fabricator's positional tolerance. The hole must be fabricated to a diameter tolerance of  $\pm t_{fab}$ .



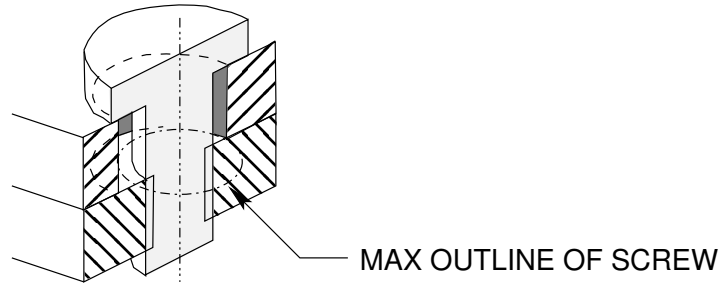


Figure 13: A Screw Through a Plate

If the fabricator can position the hole inside a diameter of  $G_{fab}$ , then the minimum working diameter of the hole is

$$D_{min} = MIN + G_{fab}.$$

The smallest possible maximum hole size is

$$D_{max} = D_{min} + 2t_{fab}$$

This value must be less than the maximum diameter specified on the drawing.

$$MAX \geq D_{max} = D_{min} + 2t_{fab} = MIN + G_{fab} + 2t_{fab}$$

For a bolted assembly,  $MIN_{bolt} = D_{bolt}$ . Your error budget is

$$\boxed{MAX_{bolt} - D_{bolt} = G + 2t.} \quad (17)$$

### A.1.2 Positional Tolerances for Screws with Zero Positional Error

In Figure 13, a screw is shown clamping two plates together. A tapped hole has no nominal clearance, so it cannot be located to a zero positional tolerance. The phantom line shows the maximum outline that could be occupied by the screw. The clearance hole is shown shifted the maximum acceptable distance, which means it is touching the maximum outline.

The nominal diameter of the screw is  $D_{scr}$ .

The fabricator can locate a hole to within a diameter of  $G_{fab}$ .

The fabricator can make the clearance hole to a tolerance of  $\pm t_{fab}$ .

$$\text{Maximum Outline } D_{MO} = D_{scr} + G_{fab}$$

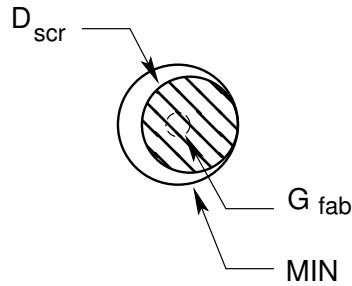


Figure 14: Minimum sized clearance hole at exact nominal

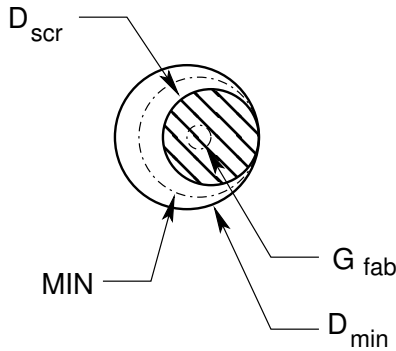


Figure 15: Minimum sized clearance hole with tolerances

Approximately as per Figure 10 , the clearance hole is specified with MIN and MAX diameters, and it is located by a positional tolerance of zero.

In Figure 14 , the screw is shown shifted the maximum distance. The clearance hole is shown at the exact nominal position, just clearing the screw.

$$\text{MIN} = D_{MO} = D_{scr} + G_{fab}$$

The fabricator can locate the clearance hole to within  $G_{fab}$ . Figure 15 shows the clearance hole shifted the maximum distance, and clearing the screw shifted the maximum distance the opposite way.

$$D_{min} = \text{MIN} + G_{fab}.$$

Since the hole can be fabricated to  $\pm t_{fab}$ , your maximum sized hole will be,

$$D_{max} = D_{min} + 2t_{fab}$$

The values  $D_{min}$  and  $D_{max}$  do not show up on fabrication drawings. They are only intermediate values, used to determine MAX.

The hole must not exceed diameter MAX. The screw must pass through it. Otherwise, you do not care. The maximum error condition is shown in Figure 13 .

The zero tolerance is applied at MMC, as shown in Figure 12 .

$$\text{MAX} = D_{max}$$

For a tapped hole of major diameter  $D$  and a maximum allowable clearance hole MAX,

$$\begin{aligned} \text{MAX} &= D_{max} \\ &= D_{min} + 2t \\ &= \text{MIN} + G + 2t \\ &= D_{scr} + G + G + 2t \\ &= D_{scr} + 2G + 2t \end{aligned}$$

$$\text{MIN} = D_{scr} + G \tag{18}$$

$$\text{MAX} = D_{scr} + 2G + 2t \tag{19}$$

If you are the designer and you specified MMC, your error budget is

$$\boxed{\text{MAX}_{scr} - D_{scr} = 2G + 2t} \tag{20}$$

If you are checking drawings, the drafter will have set the geometric tolerance of the tapped hole and defined the  $\text{MIN}_{scr}$ . Your error budget for the clearance hole is

$$\text{MAX}_{scr} - \text{MIN}_{scr} = G + 2t$$